
Fundamentals of Corrosion Mathematics and Electricity



Appalachian Underground Corrosion Short Course

Considerations

- This class concentrates on fundamental mathematical and electrical concepts
- All skills require practice regardless of what they are or how they're done
- To learn is to do
- By doing, it becomes easier



Agenda

- Units
- Circuit Theory
- Electrical Formulas
- Series and Parallel Circuit Theory



Units

- A unit is an object or thing regarded as stand alone and complete
- Can also be a component of a larger or more complex object or thing

Units

Examples of Common Units of Length

Imperial System

- Inch (in)
- Foot (ft)
- Yard (yd)
- Mile (mi)

International System (SI)

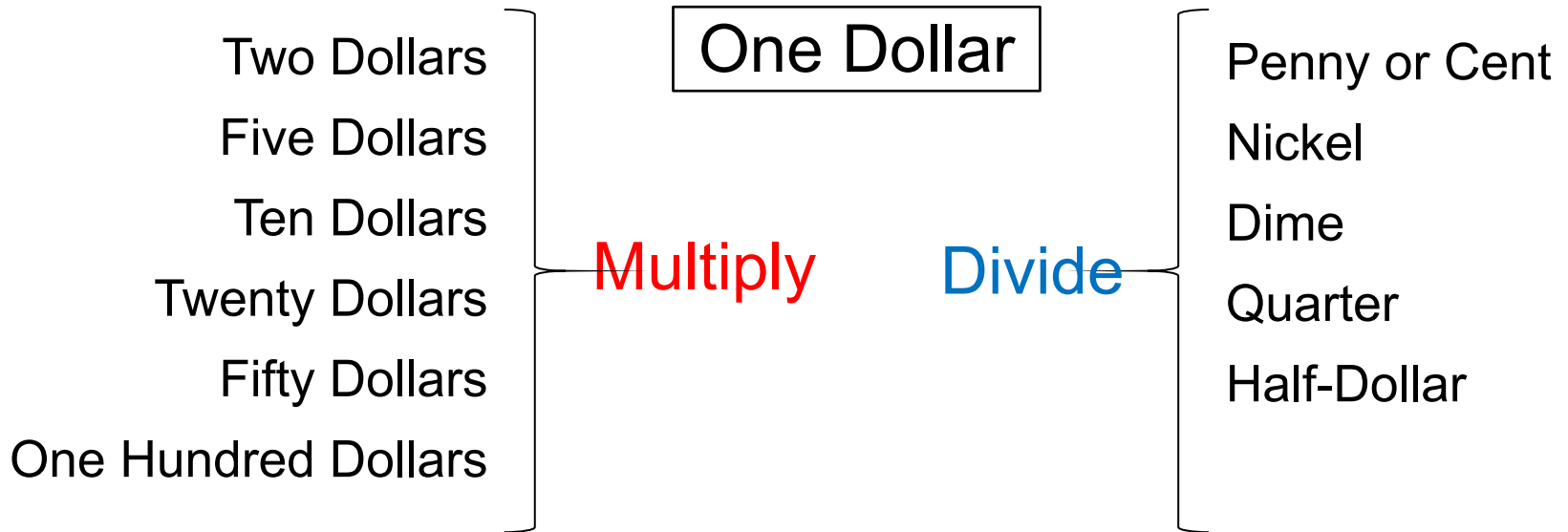
- Millimeter (mm)
- Centimeter (cm)
- Meter (m)
- Kilometer (km)

Units

Unit Nomenclature for US Money Denominations

Macro Unit

Fractional Unit



Units

Concept #1

Any number multiplied by the number 1 always equals the same number.

Examples:

$$5 * 1 = 5$$

$$354 * 1 = 354$$

$$0.75 * 1 = 0.75$$

Examples:

$$5 * 1 * 1 = 5$$

$$354 * 1 * 1 * 1 = 354$$

$$0.75 * 1 * 1 * 1 * 1 = 0.75$$



Units

Concept #2

Any number divided by itself always equals 1.

Examples:

$$\frac{6}{6} = 1$$

$$\frac{87}{87} = 1$$

$$\frac{0.375}{0.375} = 1$$

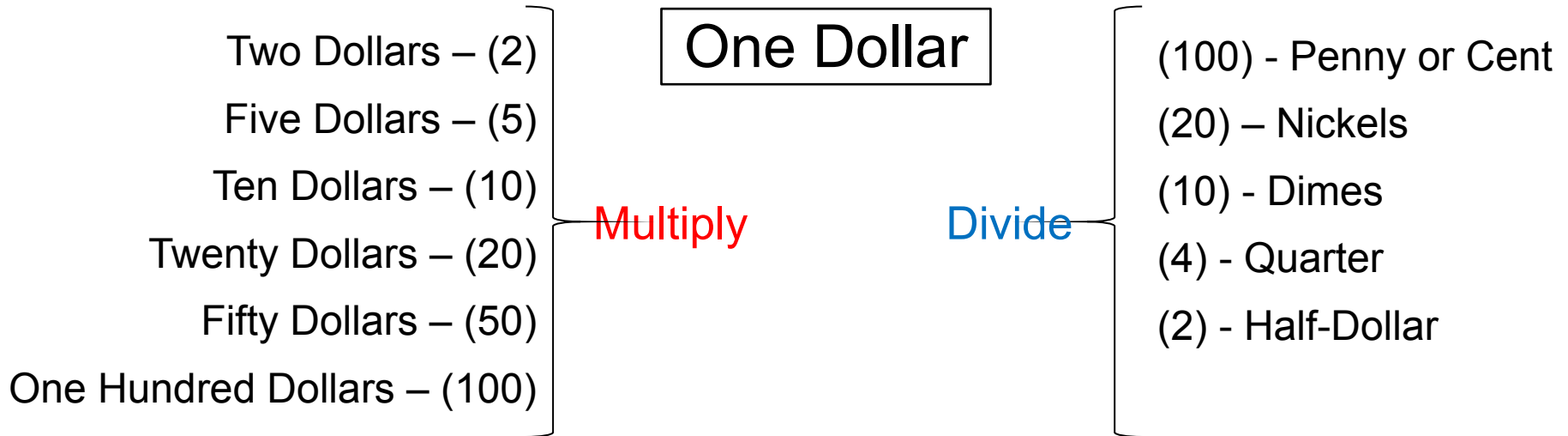


Units

Unit Nomenclature for US Money Denominations

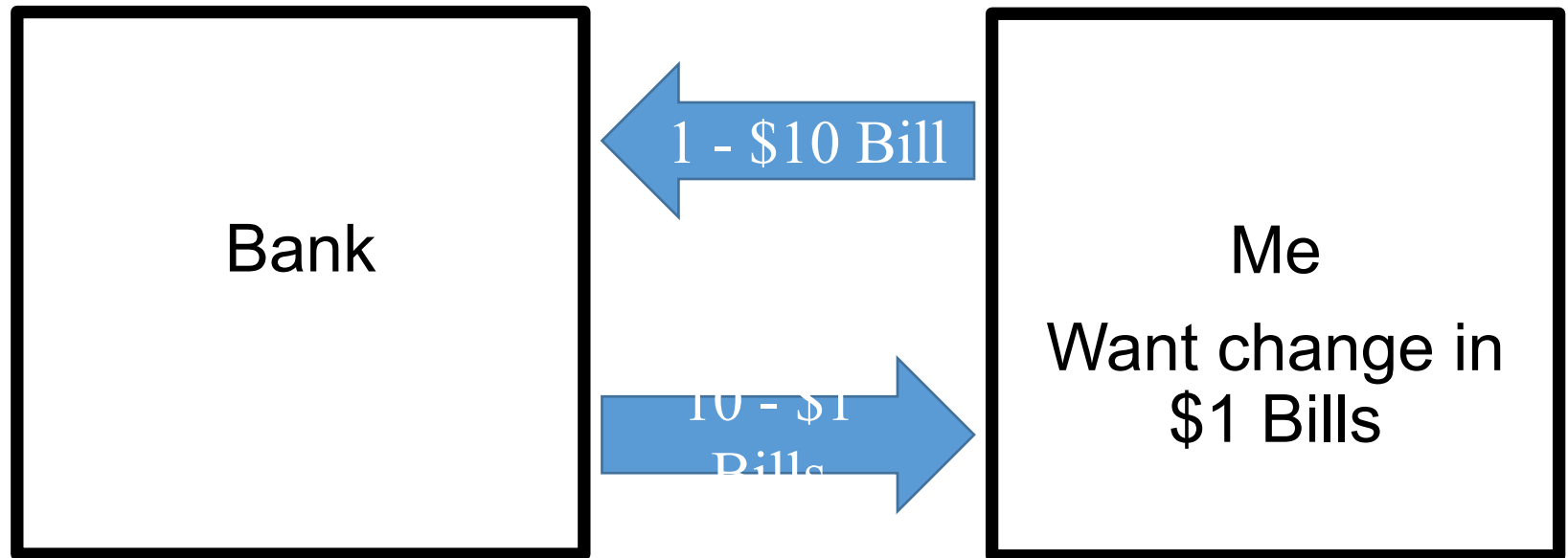
Unit

Unit



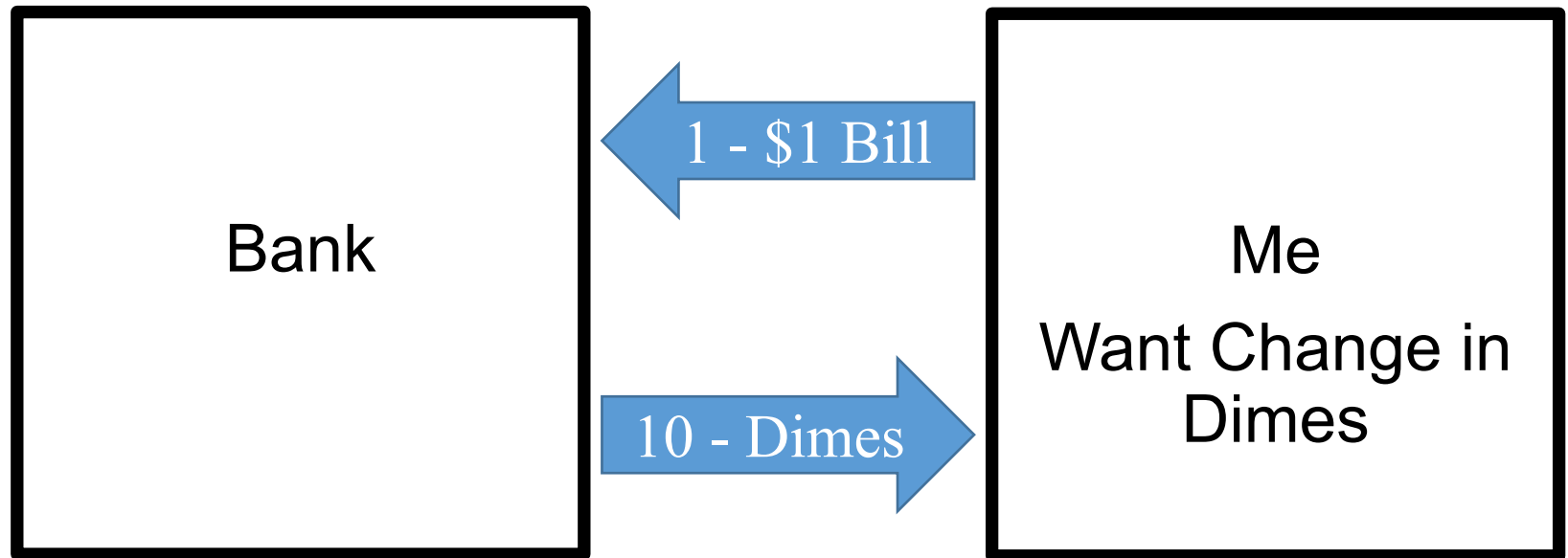
Units

Elaboration on Concept #2 – Conversion Ratio



Units

Elaboration on Concept #2 – Conversion Ratio



Units

Units Make All The Difference – Conversion Ratio

The Unit that you **want** goes on top

The Unit you **have** goes on the bottom

Example

We know there are 5280 feet in 1 mile

Conversion Ratio = **1 mile** / **5280 ft**

= 0.0001894 miles per ft **OR** 0.0001894 miles/ft



Units

Units Make All The Difference – **Conversion Ratio**

Conversion Ratio = 0.0001894 miles/ft

Question

How many miles are in 52, 864 ft?

Units

Units Make All The Difference – **Conversion Ratio**

Conversion Ratio = 0.0001894 miles/ft

We have feet and we want miles

Example

52,864 ft * 0.0001894 miles/ft

$$\frac{52,864 \text{ ft} * 0.0001894 \text{ miles}}{\text{ft}} = 10.0124 \text{ miles}$$

Units cancel.



Units

Units Make All The Difference – **Conversion Ratio**

Conversion Ratio = 1 mile / 5280 ft

We have feet and we want miles

Example

52,864 ft * 1 mile / 5280 ft

$$\frac{52,864 \text{ ft} * 1 \text{ miles}}{5280 \text{ ft}} = 10.0124 \text{ miles}$$

Units cancel.



Units

Units Make All The Difference – **Conversion Factor**

Conversion Ratio = 5280 ft / 1 mile

We have miles and we want feet

Example – Conversion Applied Backward

52,864 ft * 5280 ft / 1 mi

$$\frac{52,864 \text{ ft} * 5280 \text{ ft}}{1 \text{ mi}} = \frac{279121920 \text{ ft}^2}{\text{mile}}$$

Units don't cancel!



Units

Units Make All The Difference – Conversion Ratio

The Unit that you **want** goes on top
The Unit you **have** goes on the bottom

Example – Conversion

We have dollars and we want quarters

Ratio = 4 Quarters per Dollar

OR

4 Quarters / **1** Dollar



Units

Units Make All The Difference – Conversion Ratio

How many quarters in \$37.75

Example – Conversion

$$\frac{\$37.75 * 4 \text{ Quarters}}{\$1} = 151 \text{ Quarters}$$

Units cancel.



Units

Multiple Conversion Ratios

- 6.425 miles of pipeline
- Convert to a distance in mm
- We know the following:
 - 5280ft / 1 mile
 - 12in / 1 ft
 - 25.4mm / 1 in

$$6.425 \cancel{\text{mi}} * \frac{5280 \cancel{\text{ft}}}{1 \cancel{\text{mi}}} * \frac{12 \cancel{\text{in}}}{1 \cancel{\text{ft}}} * \frac{25.4 \text{ mm}}{1 \cancel{\text{in}}} = 10,340,035 \text{ mm}$$



Units cancel.

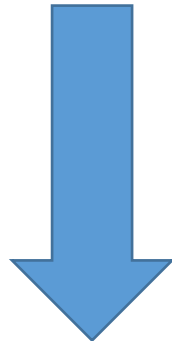
SI Units

The SI System and Layout

Getting
Bigger



Getting
Smaller



| Prefix | Symbol | Magnitude | Multiplier |
|-------------|----------|------------------------------|-------------------------|
| Tera | T | 10^{12} | x 1,000,000,000,000 |
| Giga | G | 10^9 | x 1,000,000,000 |
| Mega | M | 10^6 | x 1,000,000 |
| Kilo | K | 10^3 | x 1000 |
| Hecto | H | 10^2 | x 100 |
| Deka | Da | 10^1 | x 10 |
| Unit | -- | 1 | x 1 |
| Prefix | Symbol | Magnitude | Multiplier |
| Unit | -- | 1 | x 1 |
| Deci | d | 10^{-1} | x 0.1 |
| Centi | c | 10^{-2} | x 0.01 |
| Milli | m | 10^{-3} | x 0.001 |
| Micro | u | 10^{-6} | x 0.000001 |
| Nano | n | 10^{-9} | x 0.000000001 |
| Pico | p | 10^{-12} | x 0.000000000001 |



SI Measurement Units

The SI System and Layout

| Measurement | Unit | Symbol |
|-------------------|---------------|----------|
| Length | Meter | m |
| Mass | Gram | g |
| Volume | Liter | L |
| Time | Second | s |
| Voltage | Volt | V |
| Current | Ampere | A |
| Resistance | Ohm | Ω |
| Power | Watt | W |
| Temperature | Degree | C or K |



SI Measurement Units

Electrical Measurement Terms

| | |
|--|---|
| <h3>Voltage – Volt (V)</h3> <ul style="list-style-type: none">• Named after Alessandro Volta (Italy)• Similar in function to pressure | <h3>Current – Ampere (I)</h3> <ul style="list-style-type: none">• Named after Andre Ampere (French)• Similar in function to fluid flow |
| <h3>Resistance – Ohm (Ω)</h3> <ul style="list-style-type: none">• Named after Georg Ohm (Germany)• Similar in function to valve | <h3>Power – Watt (W)</h3> <ul style="list-style-type: none">• Named after James Watt (Scotland)• Identical in function to work |



SI Measurement Units

Electrical Measurement Terms

| | |
|--|--|
| <p>Voltage – Volt (V)</p> <ul style="list-style-type: none">• kV = 1000V• mV = 0.001V OR 1000mV per Volt• μV = 0.0000001V OR 1000μV per mV | <p>Current – Ampere (I)</p> <ul style="list-style-type: none">• kA = 1000A• mA = 0.001A OR 1000mA per Amp• μA = 0.000001A OR 1000μA per mA |
| <p>Resistance – Ohm (Ω)</p> <ul style="list-style-type: none">• GΩ = 1,000,000,000Ω OR 1000MΩ• 1 MΩ = 1,000,000Ω• 1 kΩ = 1000Ω• 1 mΩ = 0.001Ω OR 1000mΩ per Ohm• 1 $\mu\Omega$ = 0.0000001Ω OR 1000$\mu\Omega$ per mV | <p>Power – Watt (W)</p> <ul style="list-style-type: none">• GW = 1,000,000,000W OR 1000MW• MW = 1,000,000W OR 1000kW• kW = 1000W• mW = 0.001W OR 1000mW per Watt• μW = 0.0000001W OR 1000μW per mW |



SI Measurement Units

Conversion Examples

Unit you **want**

Unit you **have**

$$-0.71A * \frac{1000mA}{1A} = -710mA$$

$$1.325kV * \frac{1000V}{1kV} = 1325V$$

$$956m\Omega * \frac{1\Omega}{1000m\Omega} = 0.956\Omega$$

$$1500W * \frac{1kW}{1000W} = 1.5kW$$



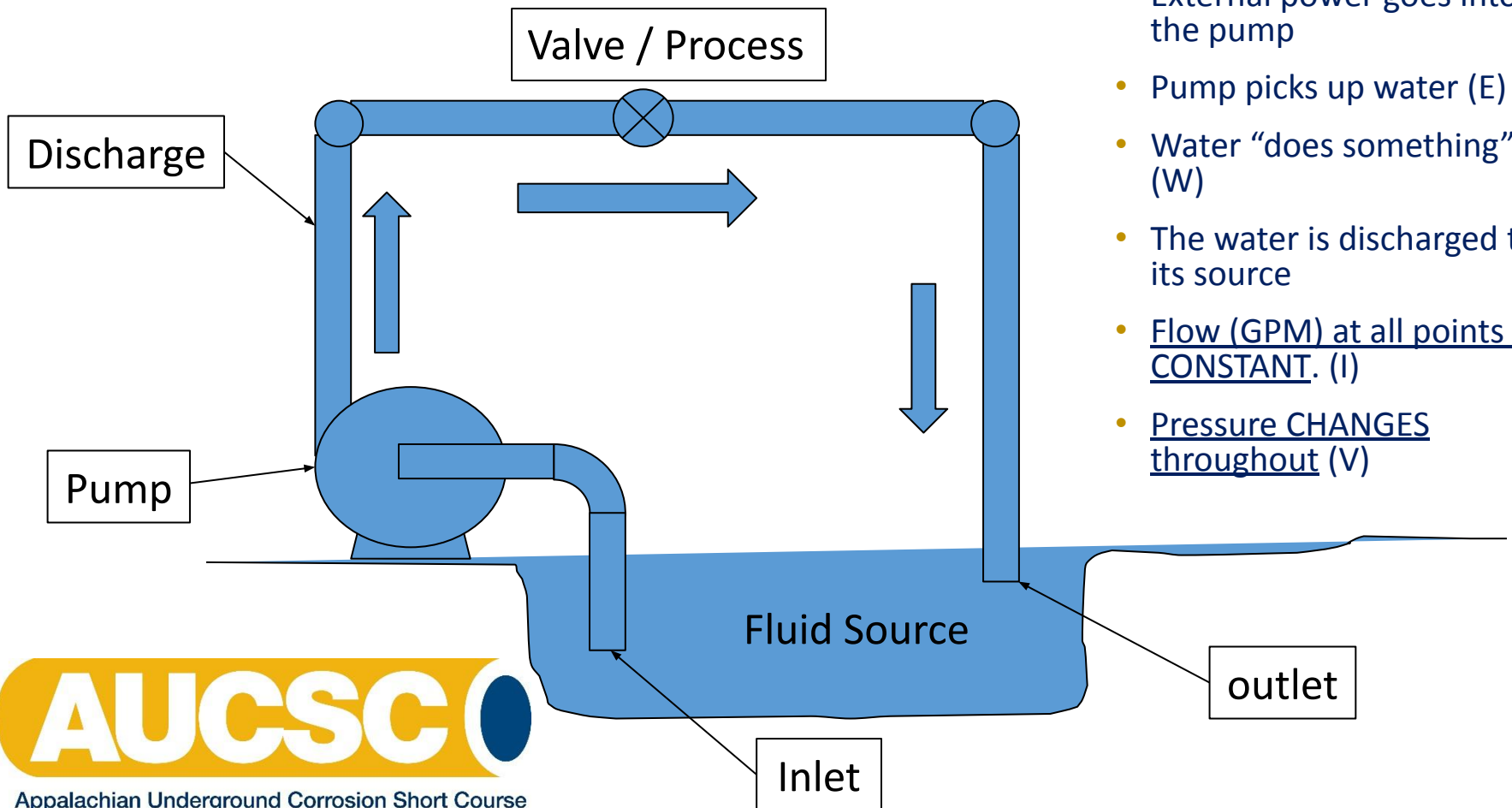
Review

- Topics
 - Skill requires practice
 - Different types of units and their relationships
 - How to derive a conversion ratio to achieve larger or smaller units of measure
 - Established some electrical units of measure



Circuits

Electric Circuits behave somewhat like fluid or pneumatic flow systems

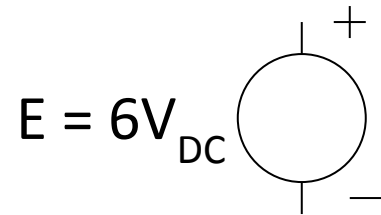
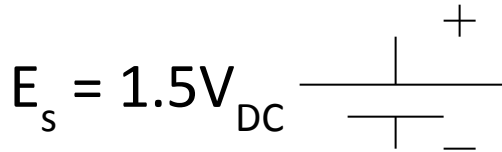


- External power goes into the pump
- Pump picks up water (E)
- Water “does something” (W)
- The water is discharged to its source
- Flow (GPM) at all points is CONSTANT. (I)
- Pressure CHANGES throughout (V)

Circuits

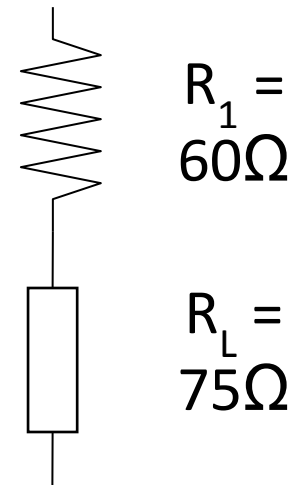
Electrical Symbols

DC Voltage Source
(Battery)



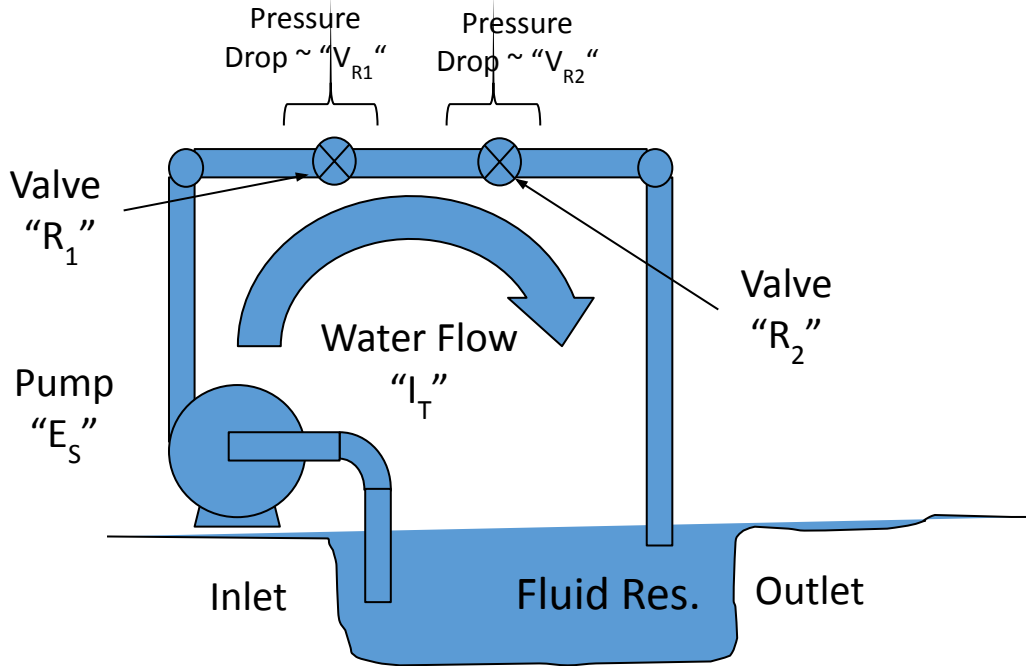
Current flow – may be represented with an arrow \longrightarrow and an “I”

Resistance – may be represented with zig-zag image or a box with or without a resistance value. Usually labeled R



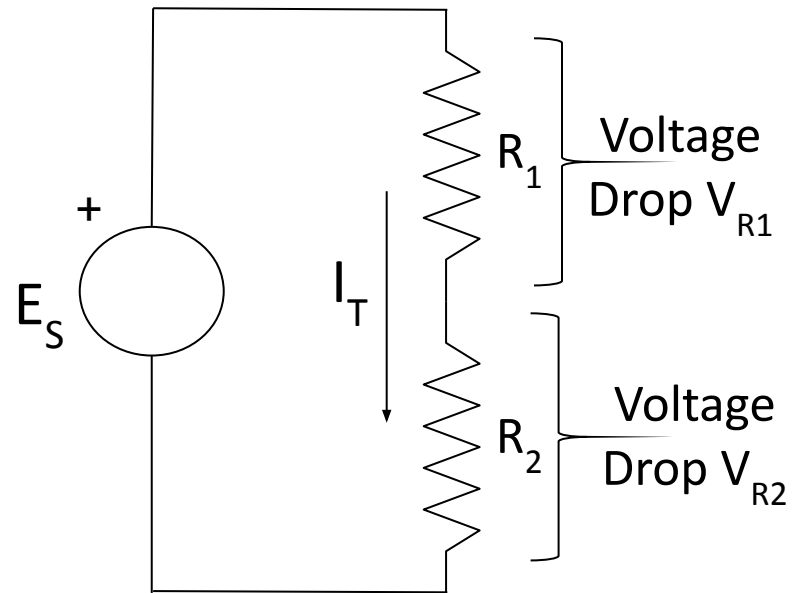
Circuits

Series Circuit - Fluid vs. Electricity



- Pressure around circuit changes
- Flow rate remains constant

- Pump Pressure \sim Source Voltage
- Water Flow \sim Electrical Current
- Valve \sim Resistor



- Voltage around circuit changes
- Current flow remains constant

Circuits

Series Circuit - Water vs. Electricity

Fluids

- **Pressure Drop**
 - Pounds per Square Inch
 - Difference between one side of flow resistance and the other
- **Flow**
 - Gallons per minute
 - Measured by Diverting the Fluid Flow

Electricity

- **Voltage Drop**
 - Volts
 - Difference between one side of flow resistance and the other
- **Current**
 - Amps
 - Measured by Diverting the Current



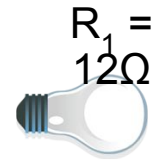
Circuits

Simple Series Circuit

- 12VDC Car Battery
- DC Lamp

Electrical current flows from battery (+) terminal through the light bulb filament back to the battery (-) terminal.

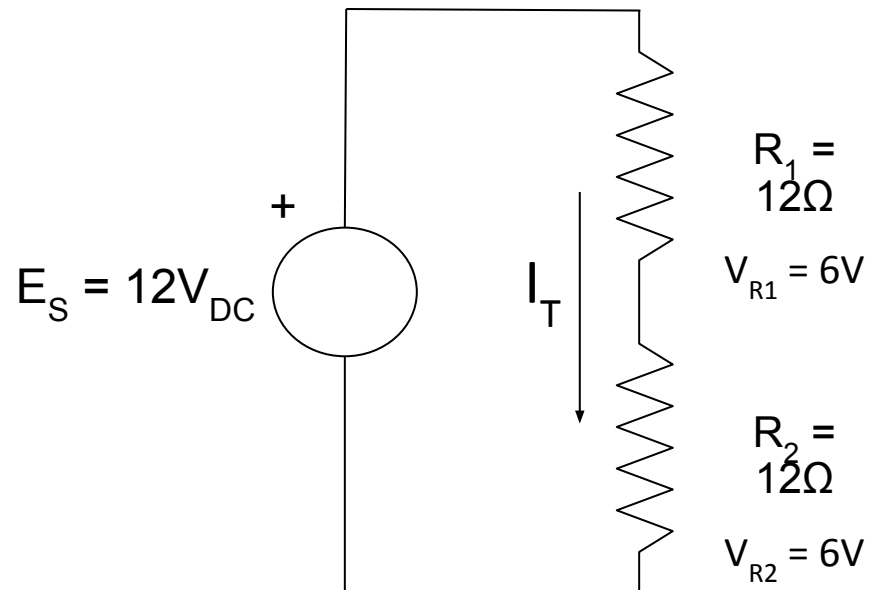
$$E_S = 12V_{DC}$$



$$R_1 = 12\Omega$$



$$R_2 = 12\Omega$$

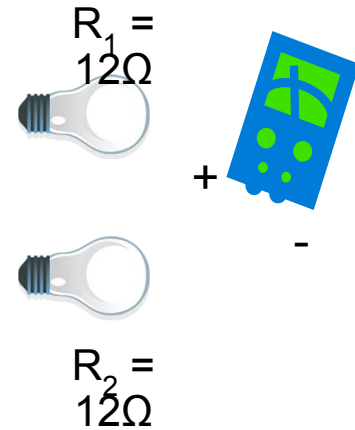
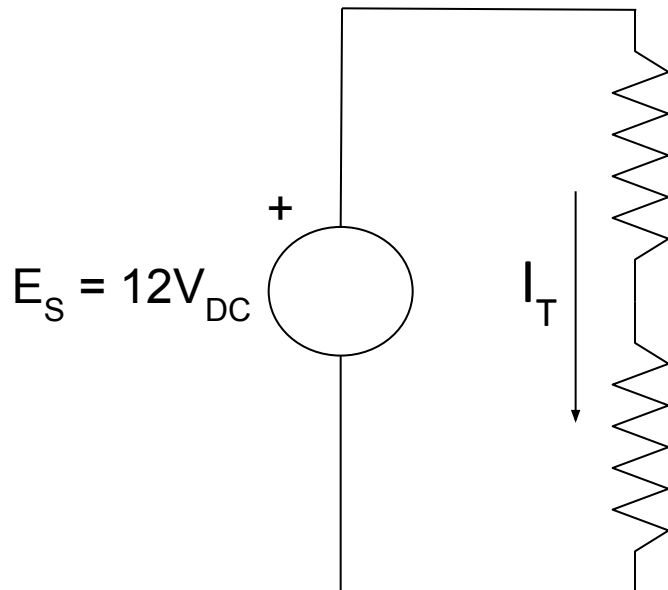


Circuits

Voltage Measurement

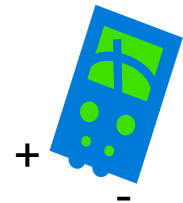
- Measure difference in voltage across the “load” or “voltage drop”
- Circuit unbroken
- Voltmeter has very high resistance (10MΩ)

$$E_S = 12V_{DC}$$



$$V_{R_2} = 6V_{DC}$$

$$R_1 = 12\Omega$$



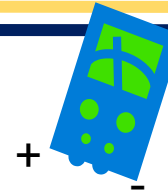
$$R_2 = 12\Omega$$

Circuits

Current Measurement

- To measure current, current must flow through the meter
- Circuit broken to insert meter
- Ammeter has very low resistance

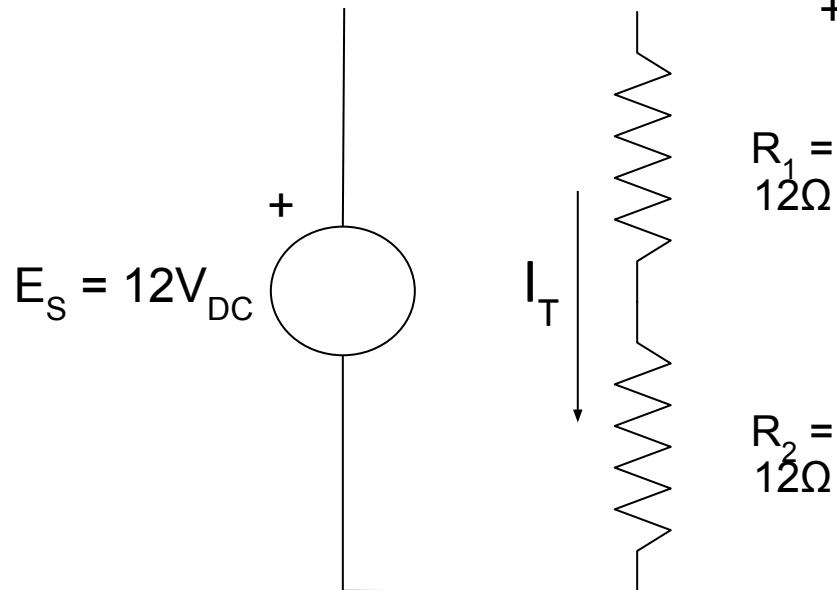
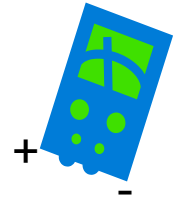
$$E_S = 12V_{DC}$$



$$I_T = 0.5A_{DC}$$



$$R_1 = R_2 = 12\Omega$$



Circuits

Circuit Breakers

- Two Types of Circuit Breakers
 - “Normal” Circuit Breaker – Breaks the circuit when the current exceeds the rating of the circuit breaker (short circuit)
 - “Ground Fault” Circuit Breaker – Breaks the circuit when the “Hot Side” (Black) current is different than the “Neutral” (White) side of the circuit

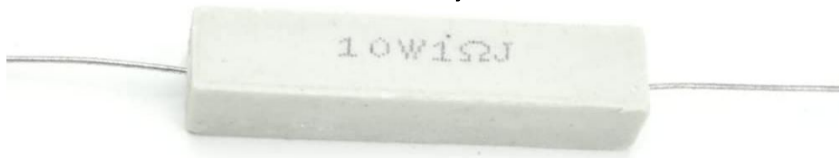


Circuits

Resistors

- Resistors are generally provided with two basic pieces of information
 - The size of the resistor in ohms
 - The wattage or maximum power the resistor can dissipate before it starts to fail

10 Watt, 1 Ω



100 Watt, 1 Ω



The Basic Electricity Formulas

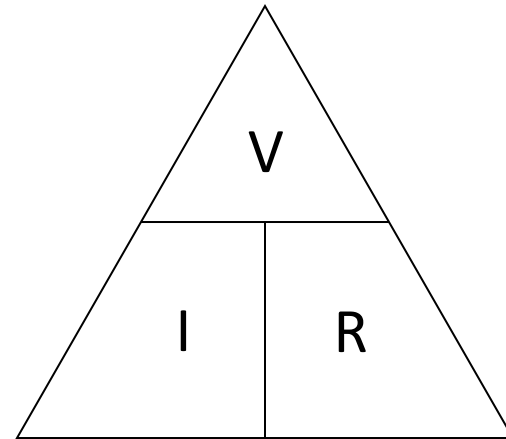
Ohms Law

A potential of 1 Volt across a resistance of 1 Ohm causes 1 ampere of current to flow

$$V = I * R$$

$$I = V / R$$

$$R = V / I$$

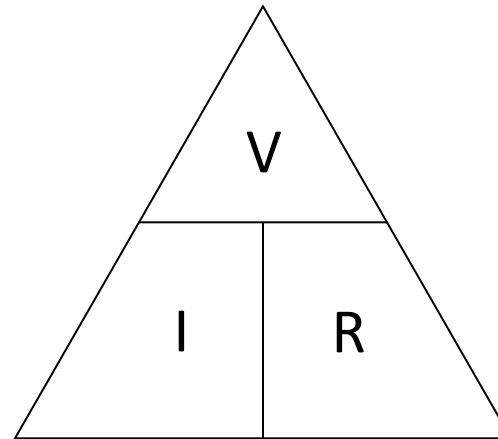


*V can be replaced with E

The Basic Electricity Formulas

Ohms Law

- Using the triangle
- Cover the unknown variable
- Known variables will be in the appropriate configuration



$$V = I * R$$

$$I = V / R$$

$$R = V / I$$

The Basic Electricity Formulas

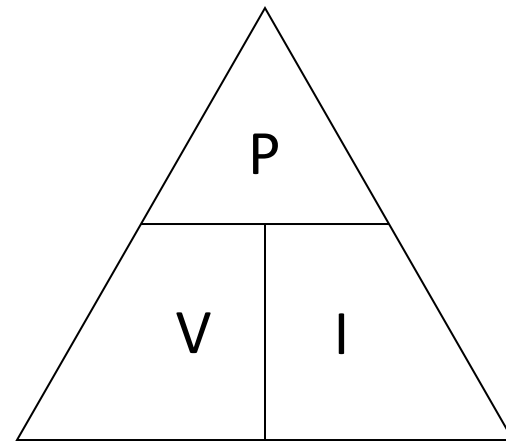
Joules Basic Power Triangle

A potential of 1 Volt across a resistance of 1 Ohm causes 1 ampere of current to flow and dissipates 1 Watt of Power

$$P = V * I$$

$$I = P / V$$

$$V = P / I$$



*V can be replaced with E

The Basic Electricity Formulas

Units, Units, Units

- For ease of calculation
- **Always** convert units to Volts, Amps, Ohms, & Watts
- Convert millivolts, milliamps, kilohms, etc. to the parent unit

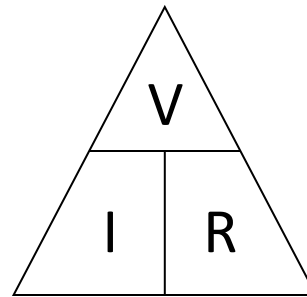
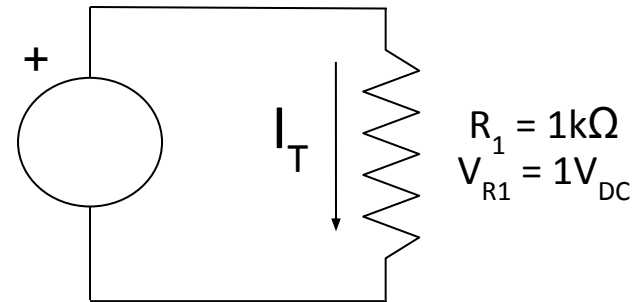


Circuit Analysis

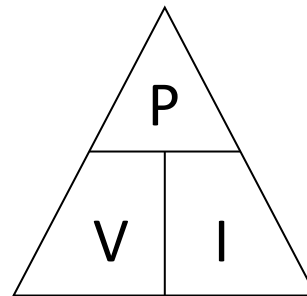
The Formulas Applied – Example 1

- The voltage (V_{R1}) across the resistance is 1 Volt
- The resistance (R_1) is $1\text{k}\Omega$ or 1000Ω
- What is the current through R_1 ?
- What is the minimum wattage for R_1 that's required?

$$E_S = 1V_{DC}$$



- $I_T = V_{R1} / R_1$
- $I_T = 1V / 1000\Omega$
- $I_T = 0.001A$ or $1mA$



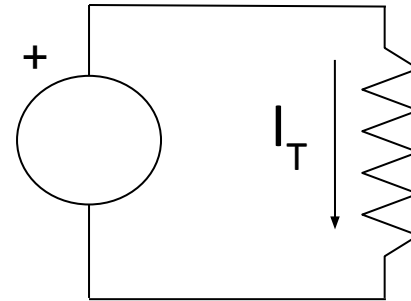
- $P_{R1} = V_{R1} * I_T$
- $P_{R1} = 1V * 0.001A$
- $P_{R1} = 0.001W$ or $1mW$

Circuit Analysis

The Formulas Applied – Example 2

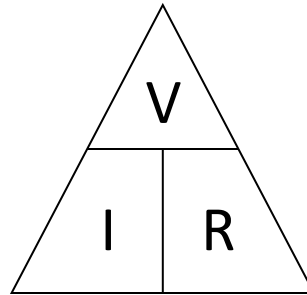
- The voltage (V_{R_1}) across the resistance is 10.5 Volts
- The resistance (R_1) is 5Ω
- What is the current through R_1 ?
- What is the minimum wattage for R_1 that's required?

$$E_S = 10.5V_{DC}$$

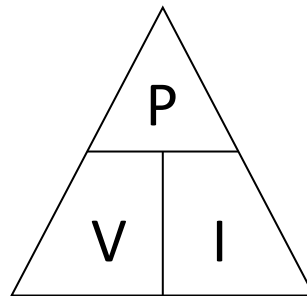


$$R_1 = 5\Omega$$

$$V_{R1} = 10.5V_{DC}$$



- $I_T = V_{R1} / R_1$
- $I_T = 10.5V / 5\Omega$
- $I_T = 2.1A$



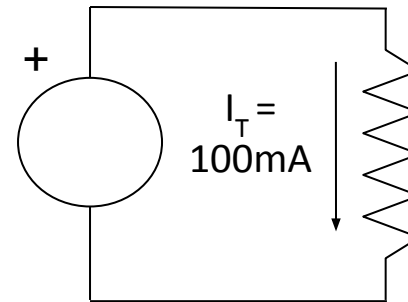
- $P_{R1} = V_{R1} * I_T$
- $P_{R1} = 10.5V * 2.5A$
- $P_{R1} = 26.25W$

Circuit Analysis

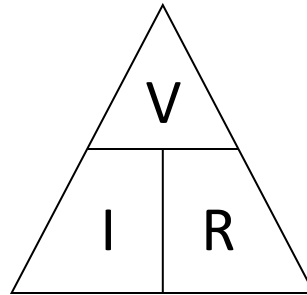
The Formulas Applied – Example 4

- The total circuit current (I_T) is 100mA
- The resistance of R_1 is 1.5 Ω
- What is the voltage across the resistance R_1 ?
- How many watts are being dissipated across R_1 ?

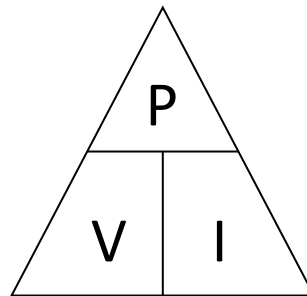
$$E_S = ? V_{DC}$$



$$R_1 = 1.5\Omega$$
$$V_{R1} = ? V_{DC}$$



- $V_{R1} = R_1 * I_T$
- $V_{R1} = 1.5\Omega * 0.1A$
- $V_{R1} = 0.15V$



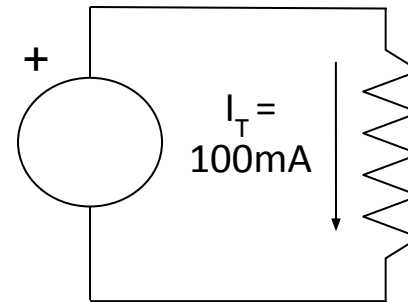
- $P_{R1} = V_{R1} * I_T$
- $P_{R1} = 0.15V * 0.1A$
- $P_{R1} = 0.015W$ or 15mW

Circuit Analysis

The Formulas Applied – Example 5 (Common Error)

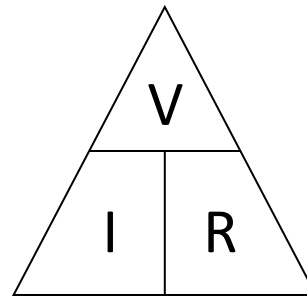
- The total circuit current (I_T) is 100mA
- The resistance of R_1 is 1.5 Ω
- What is the voltage across the resistance R_1 ?
- How many watts are being dissipated across R_1 ?

$$E_S = ? V_{DC}$$

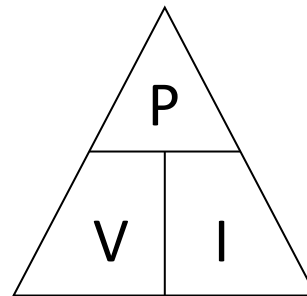


$$R_1 = 1.5\Omega$$

$$V_{R1} = ? V_{DC}$$



- $V_{R1} = R_1 * I_T$
- $V_{R1} = 1.5 * 100$
- $V_{R1} = 150V$



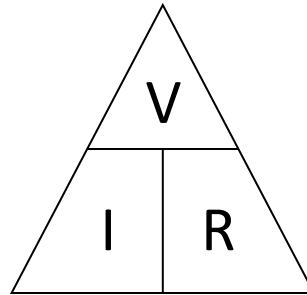
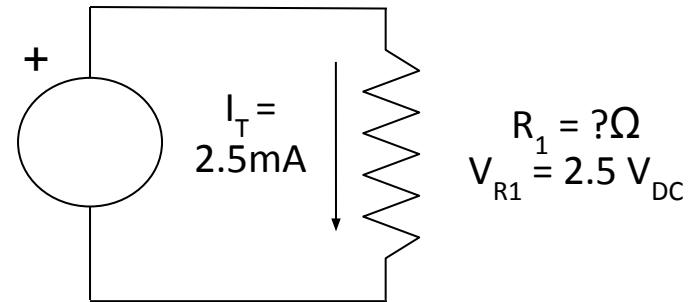
- $P_{R1} = V_{R1} * I_T$
- $P_{R1} = 150V * 100A$
- $P_{R1} = 15,000W$

Circuit Analysis

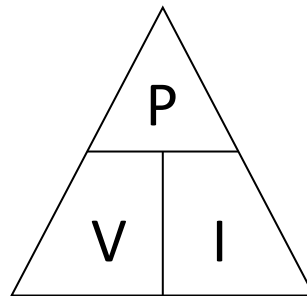
The Formulas Applied – Example 6

- The total circuit current (I_T) is 2.5mA
- The voltage across R_1 is 2.5V
- What is the value of the resistance R_1 ?
- How many watts are being dissipated across R_1 ?

$$E_S = 2.5V_{DC}$$

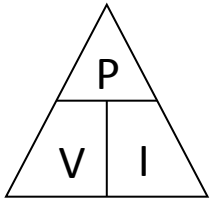


- $R_1 = VR_1 / I_T$
- $R_1 = 2.5V / 2.5mA$
- $R_1 = 1000\Omega$

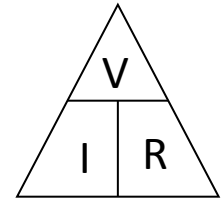


- $P_{R1} = V_{R1} * I_T$
- $P_{R1} = 2.5V * 2.5mA$
- $P_{R1} = 0.00625W$ or $6.25mW$

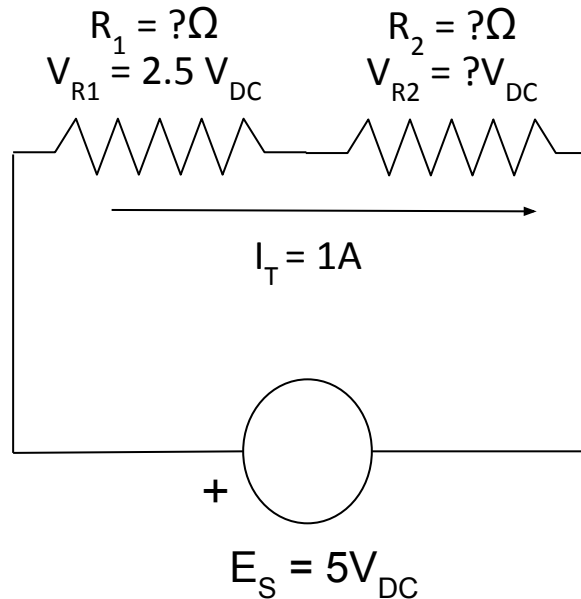
Circuit Analysis



The Formulas Applied – Example 7



- The total circuit current (I_T) is 1A
- The voltage across R_1 is 2.5V
- What is the value of the resistance R_2 ?
- How many watts are being dissipated across R_2 ?

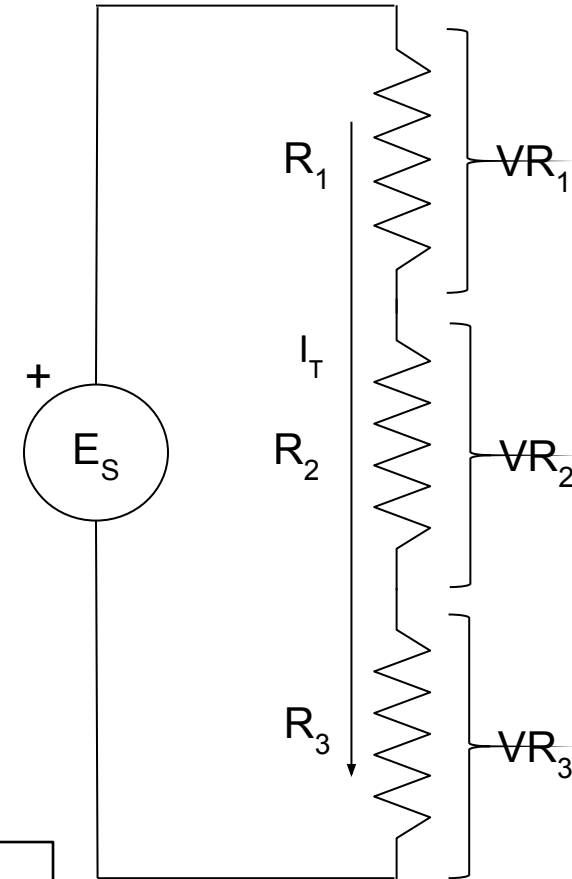


- $R_1 = V_{R1} / I_T$
- $R_1 = 2.5V / 1A$
- $R_1 = 2.5\Omega$
- $V_{R2} = E_S - V_{R1}$
- $V_{R2} = 5V - 2.5V$
- $V_{R2} = 2.5V$
- $V_{R1} = V_{R2}; R_1 = R_2$
- $R_2 = 2.5\Omega$
- $P_{R2} = V_{R1} * I_T$
- $P_{R2} = 2.5V * 1A$
- $P_{R2} = 2.5W$

Circuit Analysis

Series Circuit Analysis

- A series circuit has all elements connected “end to end” forming a single loop with the power source
- **Current (I_T) is the same through all elements**
- Voltage Drops (V_{R1} , V_{R2} , etc.) may be different
- The sum of all voltage drops = the source voltage
- $V_{R1} + V_{R2} + V_{R3} + \dots = E_S$
- Total or Equivalent circuit resistance (R_T or R_{EQ}) = the sum of all resistances



Total resistance (R_T) is always **larger** than the largest resistance

Circuit Analysis

Parallel Circuit

- A parallel circuit has all elements “side by side” forming multiple loops with the power source
- **Total Current (I_T) is the sum of currents through all elements**
- Voltage Drops (V_{R1} , V_{R2} , etc.) are the same
- $I_{R1} + I_{R2} + I_{R3} + \dots = I_T$
- Total or Equivalent circuit resistance (R_T or R_{EQ}) = the inverse of the inverse sum of all resistances

$$R_T = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots}$$



Circuit Analysis

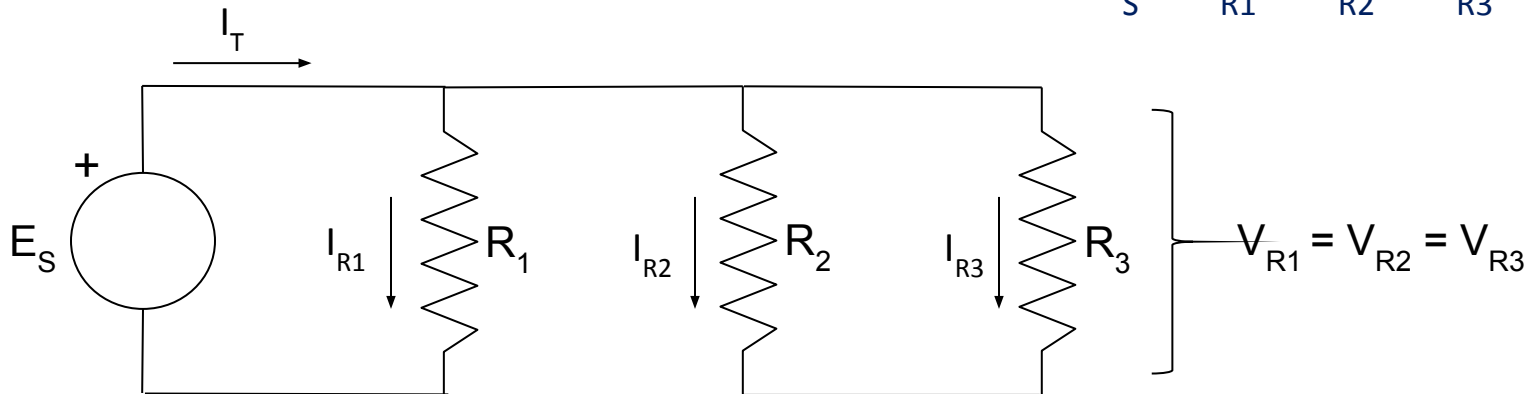
Parallel Circuit

- Each parallel current is a different magnitude
- Voltage across each parallel path or resistance is the same

- $I_T = I_{R1} + I_{R2} + I_{R3}$

- $R_T = \frac{1}{((1/R_1) + (1/R_2) + (1/R_3))}$

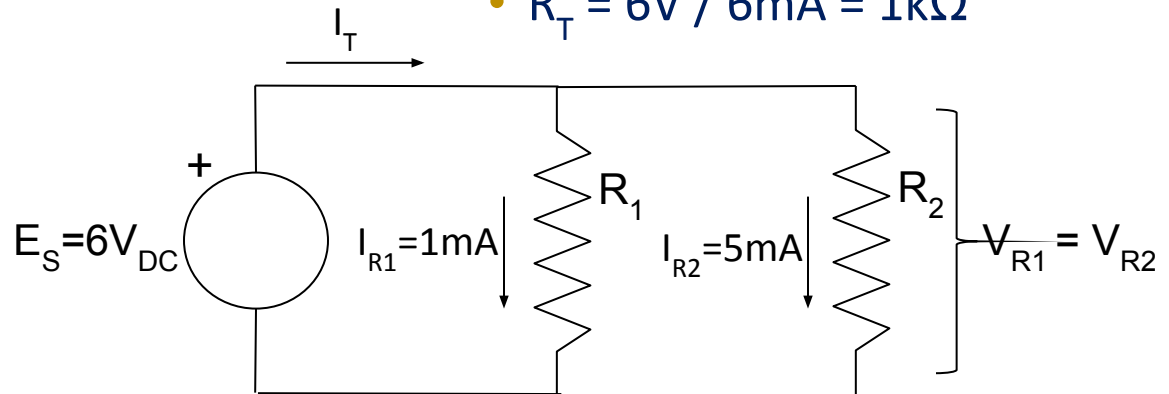
- $E_S = V_{R1} = V_{R2} = V_{R3}$



Circuit Analysis

The Formulas Applied - Example 8

- The total circuit current (I_T) is 6mA
 - The current through R_1 is 1mA & R_2 is 5mA
 - What is the value of the resistances R_1 & R_2 & R_T
 - How would you verify R_T ?
- $R_1 = V_{R1} / I_{R1}$
 - $R_1 = 6V / 0.001A = 6k\Omega$
 - $R_2 = V_{R2} / I_{R2}$
 - $R_2 = 6V / 0.005A = 1.2k\Omega$
 - $R_T = 1/((1/R_1)+(1/R_2))$
 - $R_T = 1/(0.000167s+0.000833s)$
 - $R_T = 1k\Omega$
 - $R_T = E_S / I_T$
 - $R_T = 6V / 6mA = 1k\Omega$



Thank You!

Brought to you by:

Michael Baxter

